

Using the Iterated Consensus Method, determine the complete sum of  $F(a, b, c, d) = ab'c' + a'bc' + abc' + a'b'$ . Why is the (10 points) Using the Row/Column Dominance Method, minimize  $F(a, b, c, d) = \sum m(0, 2, 5, 6, 7, 8, 9, 13) + \sum d(1, 12, 15)$ . The complete sum of  $F$  is  $F_{cs} = a'b'd' + a'cd' + a'bc + b'c' + c'd + ac' + bd$ .

- $P1 - a'b'd'$        $P3 - a'bc$        $P5 - c'd$        $P7 - bd$   
 $P2 - a'cd'$        $P4 - b'c'$        $P6 - ac'$

		P1	P2	P3	P4	P5	P6	P7
$a'b'c'd'$	m0	x			x			
$a'b'cd'$	m2	x	x					
$a'bc'd'$	m5					x		x
$a'bcd'$	m6		x	x				
$a'bcd$	m7			x				x
$ab'c'd'$	m8				x		x	
$ab'cd'$	m9				x	x	x	
$abc'd'$	m13					x	x	x

no essential prime implicants (i.e. essential columns)

		P1	P2	P3	P4	P5	P6	P7
m0	x				x			
m2	x	x						
m5						x		x
m6			x	x				
m7				x				x
m8					x		x	
m9					x	x	x	
m13						x	x	x

m9 dominates m8, remove m9  
m13 dominates m5, remove m13

		P1	P2	P3	P4	P5	P6	P7
m0	x				x			
m2	x	x						
m5						x		x
m6			x	x				
m7				x				x
m8					x		x	

P4 dominates P6, remove P6  
P7 dominates P5, remove P5

		P1	P2	P3	P4	P7
m0	x				x	
m2	x	x				
m5					x	
m6			x	x		
m7				x		x
m8					x	

		P1	P2	P3	P4	P7
m0	x				x	
m2	x	x				
m5						x
m6			x	x		
m7				x		x
m8					x	

		P1	P2	P3
m2	x	x		
m6			x	x

no dominating rows

		P1	P2	P3
m2	x	x		
m6			x	x

P2 dominates P1, remove P3  
P2 dominates P3, remove P1

P4 becomes essential to cover m8  
P7 becomes essential to cover m5

Remove essential prime implicants and the minterms they cover

		P2
m2	x	
m6	x	

P2 becomes essential to cover m2, m6

		P2
m2	x	
m6	x	

P2 becomes essential to cover m2, m6



Empty matrix – solution found!

$$F = P2 + P4 + P7$$

$$F = a'cd' + b'c' + bd$$