

# In-class Exercise 4

(PAR 8)

- Use recursive consensus method to find the complete sum of
  - $F(w, x, y, z) = wx + x'y + xyz$

$$= [x_1' + f(1, x_2, \dots, x_n)] \cdot [x_1 + f(0, x_2, \dots, x_n)]$$

- Given the following constraint matrix, use row and column dominance to determine the minimum cover

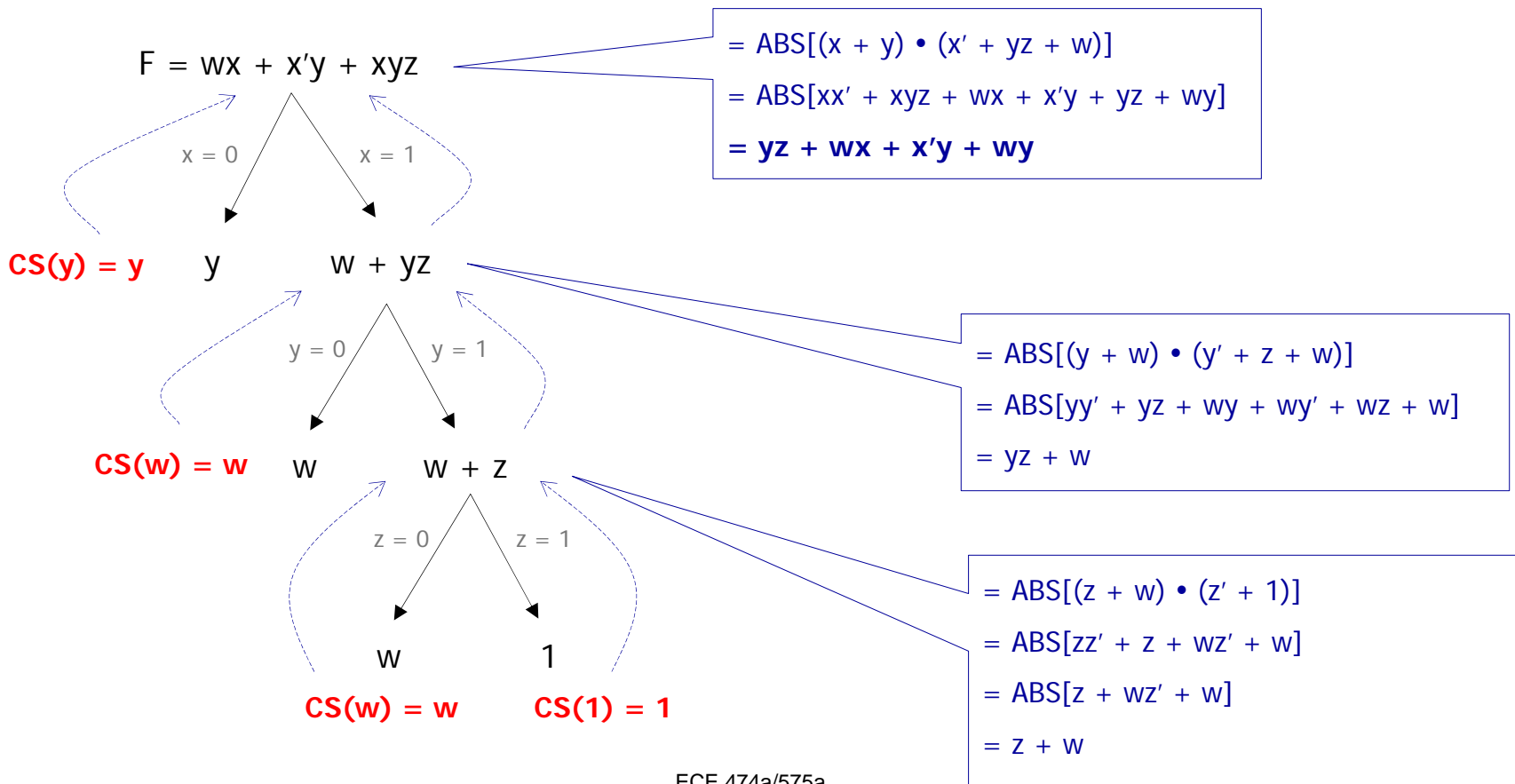
	P1	P2	P3	P4
M1	1	1	1	0
M2	1	1	0	0
M3	0	1	1	0
M4	0	1	0	1
M5	0	0	0	1

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- Use recursive consensus method to find the complete sum of
  - $F(w, x, y, z) = wx + x'y + xyz$

$$= [x_1' + f(1, x_2, \dots, x_n)] \cdot [x_1 + f(0, x_2, \dots, x_n)]$$



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- Alternative - use iterated consensus to find the complete sum

- $F(w, x, y, z) = wx + x'y + xyz$

$$F(w, x, y, z) = wx + x'y + xyz$$

$$wx + x'y \rightarrow wy$$

$$wx + xyz \rightarrow \text{NO}$$

$$x'y + xyz \rightarrow yz$$

$$F(w, x, y, z) = wx + x'y + xyz + wy + yz$$

skip pair done above

$$wx + wy \rightarrow \text{NO}$$

$$wx + yz \rightarrow \text{NO}$$

$$x'y + wy \rightarrow \text{NO}$$

$$x'y + yz \rightarrow \text{NO}$$

$$xyz + wy \rightarrow \text{NO}$$

$$xyz + yz \rightarrow \text{NO}$$

$$wy + yz \rightarrow \text{NO}$$

$$F(w, x, y, z) = wx + x'y + xyz + wy + yz$$

Remove any term contained in another term

$xyz$  in  $yz$ , remove  $xyz$

$$F(w, x, y, z) = wx + x'y + wy + yz$$

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- We can also look at the k-map to verify

F		cd			
		00	01	11	10
ab	00	0	1	3	2
	01	4	5	7	6
	11	12	13	15	14
	10	8	9	11	10

$$F(w, x, y, z) = wx + x'y + xyz$$

Not a complete sum

F		cd			
		00	01	11	10
ab	00	0	1	3	2
	01	4	5	7	6
	11	12	13	15	14
	10	8	9	11	10

$$F(w, x, y, z) = wx + x'y + yz + wy$$

Complete sum

# In-class Exercise 8 - Solution

(PAR 10)

- Given the following constraint matrix, use row and column dominance to determine the minimum cover

	P1	P2	P3	P4
M1	1	1	1	0
M2	1	1	0	0
M3	0	1	1	0
M4	0	1	0	1
M5	0	0	0	1

	P1	P2	P3	P4
M1	1	1	1	0
M2	1	1	0	0
M3	0	1	1	0
M4	0	1	0	1
M5	0	0	0	1

P4 is essential (only one to cover M5, as a bonus it also covers M4)  
Remove P4, M5, M4

	P1	P2	P3
M1	1	1	1
M2	1	1	0
M3	0	1	1

M1 dominates M2  
M1 dominates M3  
Remove M1

	P1	P2	P3
M2	1	1	0
M3	0	1	1

P2 dominates P1  
P2 dominates P3  
Remove P1, P3

	P2
M2	1
M3	1

Min Cover = P2 + P4